

# 6.270 Lecture 4

## Localization/Navigation

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# Corrections/Notes

- “8-hole pulley” → “6-hole pulley”
- Dual differential: should have mentioned that it's weaker than a standard differential drive since single motor provides all of the torque driving forward or backward rather than two motors

# Putting things together

- Yesterday, we saw how to drive in a certain direction
- In order to drive somewhere, must know where we are first (localization)
- Also want high level control of robot: should be able to say `moveToPoint(x,y)` (navigation system)

# Localization

- Difficult to navigate unless you know where you are at all times
- Tough problem:
  - Sensors noisy
  - Small errors can lead to large problems:
    - A few degrees of error can lead to 1ft of inaccuracy if you drive across the board

# A peek at localization...

- Dead reckoning: Estimate your own position based on previous estimated position and amount of change
- How?
  - Encoder – distance
  - Gyro – direction
  - Distance sensors?
  - Accelerometer?
- Why?
  - VPS updates infrequently
  - VPS updates are old (latency)
  - VPS heading isn't extremely accurate

# A peek at localization...

- We want to update our estimated position:  $x$  and  $y$
- At each time step: (pseudocode)
  - `dist = encoder_read(ENC_PORT) * CONV_FACTOR`
  - `encoder_reset(ENC_PORT)`
  - `x = x + dist*cos(theta) //use old heading`
  - `y = y + dist*sin(theta)`
  - `theta = gyro_get_degrees() % 360 //update cur heading`

# Better localization possible?

- It doesn't make sense to just ignore the VPS
- Best of both worlds?
- Dead reckoning:
  - Accurate short-term; fast updates
  - Relative changes
  - Reliable, smooth data (but drifts)
- VPS:
  - Accurate long-term (no drifting)
  - Absolute positioning
  - Potential outages, dropped packets, jitter

# How does VPS work?

- Fiducial pattern on top of your robot
- Camera mounted above playing field that tracks these patterns
- Wirelessly transmits your location to your robot





# Use VPS data too...

- Let's add some code to handle the VPS too
- When a VPS update arrives:
  - $x = \text{vps\_data.x}$
  - $y = \text{vps\_data.y}$
- This would mean VPS data is 100% trusted, since it overwrites our dead reckoning estimated position...

# Merge VPS data w/ dead reckoning

- One idea: weight VPS data and combine with existing dead-reckoning data
- When a VPS update arrives:
  - `//calculate a confidence weight`
  - `confidence = (255 - abs(motor_vel)) / 255.0`
  - $x = \text{confidence} * \text{vps\_data.x} + (1 - \text{confidence}) * x$
  - $y = \text{confidence} * \text{vps\_data.y} + (1 - \text{confidence}) * y$
- Better, but what about latency?

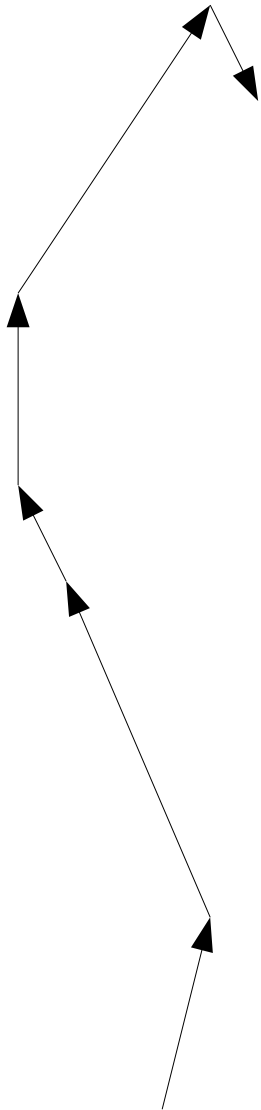
# Dealing with latency

- VPS data is inherently old – when it says “you are at  $(x,y)$ ” think of it as actually saying “*300ms ago you were at  $(x,y)$* ”
- If we store history of distance travelled and rotation amount (from dead-reckoning), can reconstruct path taken since VPS snapshot
- Apply this path to the VPS snapshot data to get an accurate estimate of where we are now

# Keeping path history

- Store a history of dead-reckoning updates (ring buffer)
- At each time step:
  - `dist = encoder_read(ENC_PORT)*CONV_FACTOR`
  - `encoder_reset(ENC_PORT)`
  - `x = x + dist*cos(theta)`
  - `y = y + dist*sin(theta)`
  - `newTheta = gyro_get_degrees() % 360`
  - `dTheta = newTheta - theta`
  - `theta = newTheta`
  - `add_to_history(dist, dTheta, current_time())`

# Path History Example



dist	dTheta	time
4	30	1000
7	0	1051
2	-12	1103
4	-12	1157
6	-110	1202

# Applying path history

- Given the VPS  $x, y, \theta$ , apply path history to get a more accurate estimate of current location
- Pseudocode:
  - Let  $\text{data\_time} = \text{time that the VPS snapshot represents} = \text{vps\_data.timestamp} - 300\text{ms}$
  - Look in path history to find first entry newer than  $\text{data\_time}$
  - Apply distance and  $d\theta$  to current location estimate
  - Repeat previous step until at end of history

# A peek at localization...

- When a VPS update arrives:
  - //calculate a confidence “weight”
  - $\text{confidence} = (255 - \text{abs}(\text{motor\_vel})) / 255.0$
  - $\text{data\_time} = \text{vps\_data.timestamp} - 300$  //300ms latency
  - $\text{dx\_since\_data} = \text{get\_total\_dx\_since}(\text{data\_time})$
  - $\text{dy\_since\_data} = \text{get\_total\_dy\_since}(\text{data\_time})$
  - $\text{vps\_x} = \text{vps\_data.x} + \text{dx\_since\_data}$
  - $\text{vps\_y} = \text{vps\_data.y} + \text{dy\_since\_data}$
  - $x = \text{confidence} * \text{vps\_x} + (1 - \text{confidence}) * x$
  - $y = \text{confidence} * \text{vps\_y} + (1 - \text{confidence}) * y$

# Basic Localization

- Just created basic sensor fusion localization code!
- Could get more advanced (e.g. Kalman filters)
- Now that we know where we are, let's go somewhere!



# Let's build a nav subsystem!

- Goal: package navigation/locomotion into self-contained system
- Navigation should run in the background (use threading) so that high level code doesn't need to worry about PID updates or dead-reckoning at all
- Abstraction!

# What should it do?

- High-level functions to drive around:
  - moveToPoint( x, y , fwd\_speed, tolerance )
  - turnToHeading( heading, ang\_speed, tolerance )
  - turnToPoint( x, y, ang\_speed, tolerance )
  - moveStraight( fwd\_speed )
  - StopMoving()
  - isMoving()
- Keep track of state of navigation system:
  - MOVING\_TO\_POINT
  - TURNING\_TO\_HEADING
  - MOVING STRAIGHT
  - STOPPED

# Why is this nice?

- Clean, easy-to-read code – drive in a square:
  - `moveToPoint(0,0, VEL, TOL)`
  - `while (isMoving()); //loop until stopped`
  - `moveToPoint(100,0, VEL, TOL)`
  - `while (isMoving());`
  - `moveToPoint(100,100, VEL, TOL)`
  - `while (isMoving());`
  - `moveToPoint(0, 100, VEL, TOL)`
  - `while (isMoving());`
  - `moveToPoint(0,0, VEL, TOL)`

# Start from the bottom

- At the lowest level, we need to set left/right motor velocities
- We would rather set forward/angular velocities – then we can have a rotation PID controller and a proportional forward velocity controller
- For `moveToPoint()`, we'll use both rotationPID and forward controller simultaneously
- For `turnToPoint()`, we'll only use rotationPID

# Setting up a nav system

- Imagine we have some “global” nav system state:
  - Float goalX
  - Float goalY
  - Float goalTheta
  - Int goalFVel
  - Int goalAVel
  - Int state = STOPPED

# Setting up a nav system

- Then high-level functions are simple – just need to set state variables for background navigation system to read
- `Void moveToPoint( x, y, fVel, tolerance)`
  - `GoalX = x`
  - `GoalY = y`
  - `GoalVel = fVel`
  - `GoalTolerance = tolerance`
  - `State = MOVING_TO_POINT`
- `Void turnToHeading( heading, aVel, tolerance)`
  - `GoalTheta = heading`
  - `GoalVel = aVel`
  - `GoalTolerance = tolerance`
  - `State = TURNING_TO_HEADING`
- `Void turnToPoint( x, y, aVel, tolerance)`
  - `heading = atan2(currentY - y, currentX - x)`
  - `turnToHeading( heading, aVel, tolerance)`

# The Navigation Process

- Main navigation loop (runs in background):
  - while(true){
    - getLocation() //dead-reckoning and VPS
    - If (state == TURN\_TO\_HEADING)
      - desiredHeading = goalHeading
    - else
      - desiredHeading = ... //use trigonometry based on goalX, goalY...
    - setRotationPIDGoal(desiredHeading);
    - UpdateRotationPID(); //sets desiredAVel
    - If (state == MOVE\_TO\_POINT)
      - DesiredFVel = ... //proportional to distance to goalX,goalY
    - Else
      - DesiredFVel = 0
    - LeftVel = desiredFVel + desiredAVel
    - RightVel = desiredFVel - desiredAVel
    - motor\_set\_vel(0, LeftVel)
    - motor\_set\_vel(1, RightVel)
    - If (state == MOVE\_TO\_POINT && distToGoal() < GoalTolerance)
      - State == STOPPED
    - If (state == TURN\_TO\_HEADING && headingError() < GoalTolerance)
      - State == STOPPED
  - }

# Minor details

- Add locks to avoid race conditions
- If heading error too large, perhaps limit forward velocity until pointed in the right direction



# Upcoming Events

- No big events today - work on your robots!
- Lecture tomorrow: Designing for Failure – 11am
- Control Systems workshop tomorrow at 3pm – have your robot ready to drive
- HappyBoards are just about ready